Amendments to the Claims:

This listing of claims will replace all prior versions, and listings, of claims in the application:

Listing of Claims:

- Currently Amended) A linear method for performing head
- motion estimation from facial feature data, the method comprising
- 3 the steps of:
- 4 obtaining a first facial image and detecting a head in said
- 5 first image;
- detecting position of not more than only four points P of said
- 7 first facial image where $P = \{p_1, p_2, p_3, p_4\}$, and $p_k = \{x_k, y_k\}$;
- 8 obtaining a second facial image and detecting a head in said
- 9 second image;
- detecting position of not more than only four points P' of
- said first second facial image where $P' = \{p'_1, p'_2, p'_3, p'_4\}$ and $p'_k = (x'_k, y'_k)$;
- 12 and
- determining the motion of the head represented by a rotation
- 14 matrix R and translation vector T using said points P and P'.

- 2. (Currently Amended) The linear method of claim 1, wherein
- 2 | said cnly four points P of said first facial image and said only
- 3 four points P' of said second facial image include locations of
- 4 outer corners of each eye and mouth of each respective first and
- 5 second facial images.
- 3. (Original) The linear method of claim 1, wherein said
- 2 head motion estimation is governed according to:

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$$\mathbf{P}_{i}' = R\mathbf{P}_{i} + \mathbf{T}$$
, where $R = \begin{bmatrix} \mathbf{r}_{i}^{T} \\ \mathbf{r}_{2}^{T} \\ \mathbf{r}_{3}^{T} \end{bmatrix} = \begin{bmatrix} r_{it} \\ r_{3}^{T} \end{bmatrix}$ and $\mathbf{T} = \begin{bmatrix} T_{1} & T_{2} & T_{3} \end{bmatrix}^{T}$ represent camera

- 4 rctation and translation respectively, said head pose estimation
- 5 being a specific instance of head motion estimation.
- 4. (Currently amended) A linear method for performing head
- 2 motion estimation from facial feature data, the method comprising
- 3 the steps of:
- d obtaining a first facial image and detecting a head in said
- 5 first image;
- 6 detecting position of four points P of said first facial image
- 7 where $P = \{p_1, p_2, p_3, p_4\}$, and $p_k = (x_k, y_k)$;
- obtaining a second facial image and detecting a head in said
- 9 second image;

detecting position of four points P' of said first second

- 11 facial image where $P' = \{p'_1, p'_2, p'_3, p'_4\}$ and $p'_k = (x'_k, y'_k)$; and,
- determining the motion of the head represented by a rotation
- 13 matrix R and translation vector T using said points P and P',
- wherein said head motion estimation is governed according to:

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$$\mathbf{P}_{i}' = R\mathbf{P}_{i} + \mathbf{T}, \text{ where } R = \begin{bmatrix} \mathbf{r}_{1}^{T} \\ \mathbf{r}_{2}^{T} \\ \mathbf{r}_{3}^{T} \end{bmatrix} = \begin{bmatrix} \mathbf{r}_{i} \end{bmatrix}_{3\times3} \text{ and } \mathbf{T} = \begin{bmatrix} T_{1} & T_{2} & T_{3} \end{bmatrix}^{T} \text{ represent camera}$$

- 16 rotation and translation respectively, said head pose estimation
- 17 being a specific instance of head motion estimation, and
- wherein said head motion estimation is governed according to
- 19 said rotation matrix R, said method further comprising the steps
- 20 of:
- determining rotation matrix R that maps points P_k to F_k for
- characterizing a head pose, said points F_1, F_2, F_3, F_4 representing three-
- 23 dimensional (3-D) coordinates of the respective four points of a
- 24 reference, frontal view of said facial image, and P_k is the three-
- 25 dimensional (3-D) coordinates of an arbitrary point where
- P_i = $[X_i \ Y_i \ Z_i]^T$, said mapping governed according to the relation:

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$$R(\mathbf{P}_2 - \mathbf{P}_1) \propto \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}^T$$

$$R(\mathbf{P}_6 - \mathbf{P}_5) \propto \begin{bmatrix} 0 & 1 & 0 \end{bmatrix}^T$$

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- wherein P_5 and P_6 are midpoints of respective line segments
- 31 connecting points P_1P_2 and P_3P_4 and, line segment connecting points
- 32 P_1P_2 is orthogonal to a line segment connecting points P_5P_6 , and
- 33 ∝indicates a proportionality factor.
- 1 5. (Original) The linear method of claim 4, wherein
- 2 components r1, r2 and r3 are computed as:

$$\mathbf{r}_2^{\tau}(\mathbf{P}_2 - \mathbf{P}_1) = 0$$

$$\mathbf{r}_1^{\mathsf{T}}(\mathbf{P}_2-\mathbf{P}_1)=0$$

$$\mathbf{r}_{1}^{T}(\mathbf{P}_{6}-\mathbf{P}_{5})=0$$

$$\mathbf{r_3}^T(\mathbf{P_6} - \mathbf{P_5}) = 0$$

- 1 6. (Original) The linear method of claim 5, wherein
- components r1, r2 and r3 are computed as:

$$r_3 = (P_6 - P_5) \times (P_2 - P_1)$$
,

$$\mathbf{r}_2 = \mathbf{r}_3 \times (\mathbf{P}_2 - \mathbf{P}_1)$$

$$\mathbf{r}_1 = \mathbf{r}_2 \times \mathbf{r}_3$$

7. (Original) The linear method of claim 4, wherein

$$\begin{bmatrix} \mathbf{P}_{i}^{T} & \mathbf{0}^{T} & \mathbf{0}^{T} & 1 & 0 & 0 \\ \mathbf{0}^{T} & \mathbf{P}_{i}^{T} & \mathbf{0}^{T} & 0 & 1 & 0 \\ \mathbf{0}^{T} & \mathbf{0}^{T} & \mathbf{P}_{i}^{T} & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{r}_{1} \\ \mathbf{r}_{2} \\ \mathbf{r}_{3} \\ \mathbf{T} \end{bmatrix} = \mathbf{P}'_{i}$$

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- 3 each point pair yielding 3 equations, whereby at least four
- 4 point pairs are necessary to linearly solve for said rotation and
- 5 translation.
- 1 8. (Original) The linear method of claim 7, further
- 2 comprising the step of: decomposing said rotation matrix R using
- 3 Singular Value Decomposition (SVD) to obtain a form $R = USV^{T}$.
- 9. (Original) The linear method of claim 7, further
- 2 comprising the step of computing a new rotation matrix according to
- $R = UV^T$
- 1 10. (Original) A linear method for performing head motion
- estimation from facial feature data, the method comprising the
- 3 steps of:
- obtaining image position of four points \mathbf{p}_k of a facial image;
- determining a rotation matrix R that maps points \mathbf{P}_k to \mathbf{F}_k for
- 6 characterizing a head pose, said points $\mathbf{F}_1, \mathbf{F}_2, \mathbf{F}_3, \mathbf{F}_4$ representing
- 7 three-dimensional (3-D) coordinates of the respective four points
- 8 of a reference, frontal view of said facial image, and \mathbf{P}_k is the

- 9 three-dimensional (3-D) coordinates of an arbitrary point where
- P_i = $[X_i \ Y_i \ Z_i]^T$, said mapping governed according to the relation:

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$$R(\mathbf{P}_2 - \mathbf{P}_1) \propto \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}^T$$

$$R(\mathbf{P}_6 - \mathbf{P}_5) \propto \begin{bmatrix} 0 & 1 & 0 \end{bmatrix}^T$$

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- wherein P_5 and P_6 are midpoints of respective line segments
- connecting points P_1P_2 and P_3P_4 and, line segment connecting points
- 16 P_1P_2 is orthogonal to a line segment connecting points P_5P_6 , and
- 17 [∞]indicates a proportionality factor.
- 1 11. (Original) The linear method of claim 10, wherein
- 2 components r1, r2 and r3 are computed as:

$$\mathbf{r}_2^T(\mathbf{P}_2 - \mathbf{P}_1) = 0$$

$$\mathbf{r}_3^T(\mathbf{P}_2-\mathbf{P}_1)=0$$

$$\mathbf{r_1}^r(\mathbf{P_6} - \mathbf{P_5}) = 0$$

$$\mathbf{r_3}^{r}(\mathbf{P_6} - \mathbf{P_5}) = 0$$

- 1 12. (Original) The linear method of claim 11, wherein
- components r1, r2 and r3 are computed as:

$$r_3 = (P_6 - P_5) \times (P_2 - P_1)$$

$$\mathbf{r}_2 = \mathbf{r}_3 \times (\mathbf{P}_2 - \mathbf{P}_1)$$

$$\mathbf{r}_1 = \mathbf{r}_2 \times \mathbf{r}_3$$

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- 1 13. The linear method of claim 12, wherein a (Original)
- motion of head points is represented according to $P'_i = RP_i + T$

$$R = \begin{bmatrix} \mathbf{r}_1^T \\ \mathbf{r}_2^T \\ \mathbf{r}_3^T \end{bmatrix} = [\mathbf{r}_{ij}]_{3\times 3}$$

represents image rotation, $T = [T_1 \quad T_2 \quad T_3]^T$

- represents translation, and P_{i}^{\prime} denotes a 3-D image position of four
- points P_k of another facial image
- 1 The linear method of claim 13, wherein

$$2 \qquad \begin{bmatrix} \mathbf{P}_{i}^{T} & \mathbf{0}^{T} & \mathbf{0}^{T} & 1 & 0 & 0 \\ \mathbf{0}^{T} & \mathbf{P}_{i}^{T} & \mathbf{0}^{T} & 0 & 1 & 0 \\ \mathbf{0}^{T} & \mathbf{0}^{T} & \mathbf{P}_{i}^{T} & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{r}_{1} \\ \mathbf{r}_{2} \\ \mathbf{r}_{3} \\ \mathbf{T} \end{bmatrix} = \mathbf{P}_{i}^{T},$$

- each point pair yielding 3 equations, whereby at least four 3
- point pairs are necessary to linearly solve for said rotation and
- translation.
- 1 15. (Original) The linear method of claim 14, further
- comprising the step of: decomposing said rotation matrix R using
- Singular Value Decomposition (SVD) to obtain a form $R = USV^{T}$.

- 1 16. (Original) The linear method of claim 15, further 2 comprising the step of computing a new rotation matrix according to $R = UV^T$
- 1 17. (Currently Amended) A program storage device readable by
- 2 machine, tangible embodying a program of instructions executable by
- 3 the machine to perform method steps for performing head motion
- 4 estimation from facial feature data, the method comprising the
- steps of:
- 6 obtaining a first facial image and detecting a head in said
- 7 first image;
- detecting position of not more than only four points P of said
- 9 first facial image where $P = \{p_1, p_2, p_3, p_4\}$, and $p_k = (x_k, y_k)$;
- obtaining a second facial image and detecting a head in said
- 11 second image;
- detecting position of not more than only four points P' of
- said first second facial image where $P' = \{p'_1, p'_2, p'_3, p'_4\}$ and $p'_k = (x'_k, y'_k)$;
- 14 and,
- determining the motion of the head represented by a rotation
- 16 matrix R and translation vector T using said points P and P'.

- 1 18. (Currently amended) The program storage device readable
 2 by machine as claimed in claim 17, wherein said only four points P
 3 of said first facial image and only four points P' of said second
 4 facial image include locations of outer corners of each eye and
 5 mouth of each respective first and second facial image.
- 1 19. (Original) The program storage device readable by
 2 machine as claimed in claim 17, wherein said head motion estimation
 3 is governed according to:

$$R = \begin{bmatrix} \mathbf{r}_1^T \\ \mathbf{r}_2^T \\ \mathbf{r}_3^T \end{bmatrix} = \begin{bmatrix} \mathbf{r}_{ij} \end{bmatrix}_{j \neq 3}$$

$$\mathbf{T} = \begin{bmatrix} \mathbf{r}_{ij} \\ \mathbf{r}_{ij} \end{bmatrix}^T \quad \text{represent}$$
and

- 5 camera rotation and translation respectively, said head pose
- 6 estimation being a specific instance of head motion estimation.
- 20. (Previously presented) A program storage device
- 2 readable by machine, tangible embodying a program of instructions
- 3 executable by the machine to perform method steps for performing
- 4 head motion estimation from facial feature data, the method
- 5 comprising the steps of:
- 6 obtaining a first facial image and detecting a head in said
- 7 first image;

- 8 detecting position of four points P of said first facial image
- 9 where $P = \{P_1, P_2, P_3, P_4\}$, and $P_k = (x_k, y_k)$;
- obtaining a second facial image and detecting a head in said
- 11 second image;
- detecting position of four points P' of said first second
- facial image where $P' = \{p'_1, p'_2, p'_3, p'_4\}$ and $p'_k = (x'_k, y'_k)$; and
- determining the motion of the head represented by a rotation
- 15 matrix R and translation vector T using said points P and P',
- wherein said head motion estimation is governed according to:

$$R = \begin{bmatrix} \mathbf{r}_1^T \\ \mathbf{r}_2^T \\ \mathbf{r}_3^T \end{bmatrix} = \begin{bmatrix} \mathbf{r}_{ij} \end{bmatrix}_{3x3}$$

$$\mathbf{P}_i' = R\mathbf{P}_i + \mathbf{T}, \quad \text{where} \quad \mathbf{T} = \begin{bmatrix} \mathbf{r}_{ij} \\ \mathbf{r}_{ij} \end{bmatrix}$$
and
$$\mathbf{T} = \begin{bmatrix} \mathbf{r}_{ij} \\ \mathbf{r}_{ij} \end{bmatrix}$$

- 18 camera rotation and translation respectively, said head pose
- estimation being a specific instance of head motion estimation, and
- wherein said head pose estimation is governed according to
- 21 said rotation matrix R, said method further comprising the steps
- 22 of:
- 23 determining rotation matrix R that maps points P_k to F_k for
- characterizing a head pose, said points $\mathbf{F_1}, \mathbf{F_2}, \mathbf{F_3}, \mathbf{F_4}$ representing three-
- 25 dimensional (3-D) coordinates of the respective four points of a
- reference, frontal view of said facial image, and P_k is the three-

- 27 dimensional (3-D) coordinates of an arbitrary point where
- 28 $P_i = [X_i \ Y_i \ Z_i]^T$, said mapping governed according to the relation:

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$$R(\mathbf{P}_2 - \mathbf{P}_1) \propto \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}^T$$
$$R(\mathbf{P}_6 - \mathbf{P}_5) \propto \begin{bmatrix} 0 & 1 & 0 \end{bmatrix}^T$$

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- wherein P_5 and P_6 are midpoints of respective line segments
- connecting points P_1P_2 and P_3P_4 and, line segment connecting points
- P_1P_2 is orthogonal to a line segment connecting points P_5P_6 , and
- 35 cindicates a proportionality factor.
- 1 21. (Previously presented) The program storage device
- 2 readable by machine as claimed in claim 20, wherein components r1,
- 3 r2 and r3 are computed as:

$$\mathbf{r}_{2}^{T}(\mathbf{P}_{2}-\mathbf{P}_{1})=0$$

$$\mathbf{r}_3^T(\mathbf{P}_2-\mathbf{P}_1)=0$$

$$\mathbf{r_1}^T(\mathbf{P_6} - \mathbf{P_5}) = 0$$

$$\mathbf{r_3^7}(\mathbf{P_6}-\mathbf{P_5})=0$$

- 1 22. (Previously presented) The program storage device
- 2 readable by machine as claimed in claim 20, wherein components r1,
- 3 r2 and r3 are computed as:

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$$r_5 = (P_6 - P_5) \times (P_2 - P_1)$$

$$\mathbf{r}_2 = \mathbf{r}_3 \times (\mathbf{P}_2 - \mathbf{P}_1)$$

$$\mathbf{r}_1 = \mathbf{r}_2 \times \mathbf{r}_3$$

- 1 23. (Previously presented) The program storage device
- 2 readable by machine as claimed in claim 20, wherein

$$\begin{bmatrix} \mathbf{P}_{i}^{T} & \mathbf{0}^{T} & \mathbf{0}^{T} & \mathbf{1} & \mathbf{0} & \mathbf{0} \\ \mathbf{0}^{T} & \mathbf{P}_{i}^{T} & \mathbf{0}^{T} & \mathbf{0} & \mathbf{1} & \mathbf{0} \\ \mathbf{0}^{T} & \mathbf{0}^{T} & \mathbf{P}_{i}^{T} & \mathbf{0} & \mathbf{0} & \mathbf{1} \end{bmatrix} \begin{bmatrix} \mathbf{r}_{1} \\ \mathbf{r}_{2} \\ \mathbf{r}_{3} \\ \mathbf{T} \end{bmatrix} = \mathbf{P}_{i}^{T}$$

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- each point pair yielding 3 equations, whereby at least four
- 5 point pairs are necessary to linearly solve for said rotation and
- 6 translation.
 - 24. (Previously presented) The program storage device readable by machine as claimed in claim 23, further comprising the steps of decomposing said rotation matrix R using Singular Value Decomposition (SVD) to obtain a form $R = USV^T$.
 - 25. (Previously presented) The program storage device readable by machine as claimed in claim 23, further comprising the steps of computing a new rotation matrix according to $R = UV^T$.